

# Magnetic phases for spinor bosons in the cavity

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As experimental trapping of ultracold spinor bosonic gases in high-finesse optical cavities continues to advance, there is a growing need for theoretical studies of the corresponding extended Bose–Hubbard models with two-component bosons. Here, we investigate the simplest case of cavity-induced interactions that arise when the nodes of the optical lattice coincide with the antinodes of the cavity field. We analyze the system within mean-field theory in the grand-canonical ensemble. In the atomic limit, the homogeneous system hosts two insulating magnetic phases: an anti ferromagnet (AFM) and a spin density wave (SDW). When tunneling is introduced, these phases become surrounded by a superfluid phase and three distinct supersolid phases, distinguished by different patterns of spin and density imbalances between odd and even sites. Finally, we include a harmonic trapping potential with a fixed magnetization constraint in our simulations, which allows us to obtain the full phase diagram directly relevant for experiments, revealing plethora of different phases that could be observed in a trap.

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